

Message Authentication (消息认证)

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- 2 Message Authentication Code
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- 3 Constructing Secure MACs
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Questions about message integrity

To enforce **secure communication** is more than protecting **message secrecy**, we may also encounter the following **message integrity/authenticity** questions:

- How can you be sure the message (e.g. emails, SMS, etc.) is from the sender it claims to be from?
- How can you be sure the message's content is intact?



图 1: “Boss” sends you a message¹

¹Pic from Internet

例 (An “encrypt-to-authenticate” scheme)

Consider the setting where Alice and Bob share a secret key/pad k .

- 1 To authenticate her message, Alice encrypts its message m by $c := m \oplus k$ and sends it to Bob.
- 2 To verify the message's authenticity, Bob decrypts to get a message m' and checks whether it “looks good” (e.g. whether it's properly formatted and meaningful).

Q: Does this scheme work?

例 (An “encrypt-to-authenticate” scheme)

Consider the setting where Alice and Bob share a secret key/pad k .

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 - 2 To verify the message's authenticity, Bob decrypts to get a message m' and checks whether it “looks good” (e.g. whether it's properly formatted and meaningful).
- The adversary Eve can **flip any bits of the message**. If Eve knows the message format, she can modify the message without causing any suspicions of Bob.
 - For message integrity authentication, **encryption DOES NOT directly solve** our problem.

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Attach a tag to authenticate

In our daily lives, tags are often used to authenticate a variety of objects:

- Brand tags for merchandises (e.g. clothes, shoes, bags, foods, etc.)
- Name tags for animals (e.g. cats, dogs, etc.)
- Stamps for documents (e.g. letters, certificates, etc.)
-



图 2: The authentication tag of Yangcheng Lake Crab

Use a “tag” to authenticate messages

Q: Can we apply the “attach-a-tag” idea to solve our problem?

A: Yes, we can use a special tag called **Message Authentication Code** (消息认证码) or **MAC**.

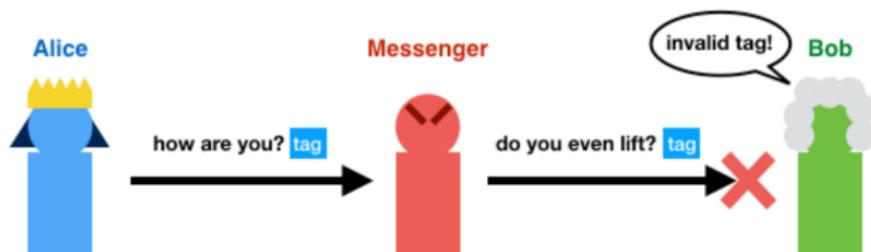


图 3: Use a MAC tag to authenticate messages²

²Pic from <https://livebook.manning.com/book/real-world-cryptography/>

DEFINITION 4.1

A **message authentication code** (or **MAC**) Π consists of three probabilistic polynomial-time algorithms ($Gen, Mac, Vrfy$):

- 1 The **key-generation algorithm** Gen takes as input the security parameter 1^n and outputs a key k with $|k| \geq n$.
- 2 The **tag-generation algorithm** Mac takes as input a key k and a message $m \in \{0, 1\}^*$, and outputs a tag t :

$$t \leftarrow Mac_k(m) \text{ or } t := Mac_k(m).$$

- 3 The **deterministic verification algorithm** $Vrfy$ takes as input a key k and a message m and a tag t , it outputs a bit b , with $b = 1$ meaning **valid** and $b = 0$ meaning **invalid**:

$$b := Vrfy_k(m, t).$$

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- **Correctness:** it is required that for every n , every key k output by $Gen(1^n)$, and every $m \in \{0, 1\}^*$, it holds that

$$Vrfy_k(m, Mac_k(m)) = 1.$$

- When Mac is deterministic, a **canonical way** to perform verification, which is actually often used, is to simply **recompute the tag and check for equality**.

The message authentication experiment

The **security** is defined via the following experiment for a message authentication scheme $\Pi = (Gen, Mac, Vrfy)$:

The message authentication experiment $Mac\text{-}forge_{\mathcal{A},\Pi}(n)$:

- 1 A key k is generated by running $Gen(1^n)$ and kept secret from the adversary.
- 2 The adversary \mathcal{A} is given input 1^n and oracle access to $Mac_k(\cdot)$. The adversary eventually outputs (m, t) . Let \mathcal{Q} denote the set of queries that \mathcal{A} asked its oracle.
- 3 \mathcal{A} succeeds iff (1) $Vrfy_k(m, t) = 1$ and (2) $m \notin \mathcal{Q}$. In that case, the output of the experiment is defined to be 1 and written as:

$$Mac\text{-}forge_{\mathcal{A},\Pi}(n) = 1.$$

DEFINITION 4.2

A message authentication code $\Pi = (Gen, Mac, Vrfy)$ is **existentially unforgeable under an adaptive chosen-message attack** or just **secure**, if for all PPT adversaries \mathcal{A} , there is a negligible function $negl$ such that:

$$Pr[Mac-forge_{\mathcal{A}, \Pi}(n) = 1] \leq negl(n).$$

- A **secure MAC** ensures that an adversary cannot generate a valid tag on **any new message that was never previously authenticated**.

Strongly secure MAC

- Recall a secure MAC ensures that an adversary cannot generate a valid tag on a **new message** that was never previously authenticated.
- Nevertheless, a secure MAC does not ensure that the adversary cannot generate a **new tag** on a previously authenticated message.
- A **strongly secure** MAC can rule out the above “weakness”³.

³In general, this type of “weakness” is not a concern. Nevertheless, in some settings it is useful to consider a stronger security.

Definition of strong MACs

We define a similar experiment called *Mac-sforge*:

The message authentication experiment $Mac\text{-}sforge_{\mathcal{A},\Pi}(n)$:

- 1 A key k is generated by running $Gen(1^n)$.
- 2 The adversary \mathcal{A} is given input 1^n and oracle access to $Mac_k(\cdot)$. The adversary eventually outputs (m, t) . Let \mathcal{Q} denote the set of **pairs of queries that \mathcal{A} asked its oracle and their corresponding responses**.
- 3 \mathcal{A} succeeds iff (1) $Vrfy_k(m, t) = 1$ and (2) $(m, t) \notin \mathcal{Q}$. In that case, the output of the experiment is defined to be 1 and written as:

$$Mac\text{-}sforge_{\mathcal{A},\Pi}(n) = 1.$$

Definition of strong MACs

DEFINITION 4.3

A message authentication code $\Pi = (\text{Gen}, \text{Mac}, \text{Vrfy})$ is **strongly secure**, or a **strong MAC**, if for all PPT adversaries \mathcal{A} , there is a negligible function negl such that:

$$\Pr[\text{Mac-sforge}_{\mathcal{A}, \Pi}(n) = 1] \leq \text{negl}(n).$$

PROPOSITION 4.4

Let $\Pi = (\text{Gen}, \text{Mac}, \text{Vrfy})$ is a secure MAC that uses canonical verification. Then Π is a strong MAC.

- In fact, all real-world MACs use canonical verification.

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How to use a secure MAC?

- For each message m , Sender sends $\langle m, t = MAC_k(m) \rangle$ to Receiver.
- Receiver runs $Vrfy(m, t)$. If verification passes, accepts m and adds m to Q . Otherwise, reject m .

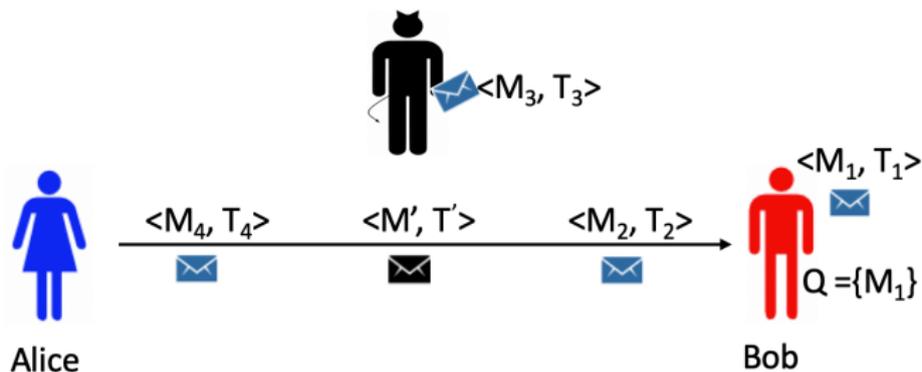


图 4: Alice sends M_1, M_2, M_3, M_4 one by one to Bob. The attacker intercepts M_2 and replace it with M' .

How to handle repeated messages with a secure MAC?

What if Alice needs to send a message in \mathcal{Q} , (i.e. was sent previously)?

- Directly applying the MAC would cause repeated messages to be **rejected**.
- One can append a unique **timestamp** or **nonce** to each message.

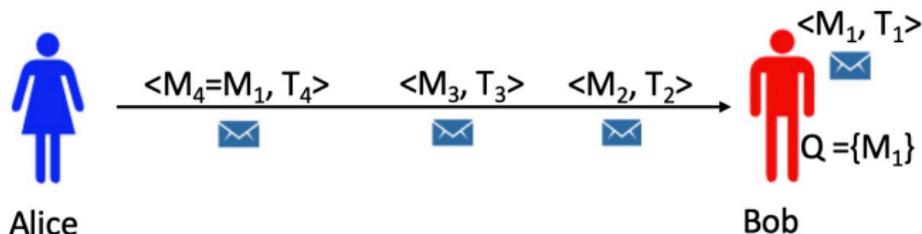


图 5: M_4 would be rejected by Bob when directly applying MAC

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Constructing a fixed-length MAC with PRFs

- A **fixed-length MAC**: If there is a function l such that for every k output by $Gen(1^n)$, Mac_k is **ONLY** defined for message $m \in \{0, 1\}^{l(n)}$, we call the scheme a *fixed-length MAC for messages of length $l(n)$* .
- Basic idea: If the MAC tag t is obtained by applying a PRF to a message m , then forging a tag on a previously unauthenticated message requires the adversary to correctly guess the output of the PRF at a “new” input. However, **this is infeasible for any PPT adversaries**.

CONSTRUCTION 4.5

Let F be a PRF. Define a fixed-length MAC for message of length n as follows:

- *Mac*: on input a key $k \in \{0, 1\}^n$ and a message $m \in \{0, 1\}^n$, output the tag: $t := F_k(m)$.
- *Vrfy*: on input a key $k \in \{0, 1\}^n$, a message $m \in \{0, 1\}^n$, and a tag $t \in \{0, 1\}^n$, output 1 iff $t = F_k(m)$.

THEOREM 4.6

If F is a PRF, then Construction 4.5 is a secure fixed-length MAC for message of length n .

Proof Sketch:

First, we construct a new ideal scheme $\tilde{\Pi}$ by replacing the PRF in Construction 4.5 with a real random function. We know

$$\Pr[\text{Mac-forge}_{\mathcal{A}, \tilde{\Pi}}(n) = 1] \leq 2^{-n}. \quad (1)$$

Q: Why?

Security analysis of Construction 4.5 (Contd.)

Proof Sketch (Contd.):

Next, due to the definition of PRF, we know the *Mac-forge* experiment cannot differentiate Π (which is built with a PRF) and $\tilde{\Pi}$ (which is built with a real random function), i.e.

$$|Pr[Mac\text{-}forge_{\mathcal{A},\Pi}(n) = 1] - Pr[Mac\text{-}forge_{\mathcal{A},\tilde{\Pi}}(n) = 1]| \leq \text{negl}(n). \quad (2)$$

Q: Why?

Summarizing (1) and (2), we know

$$Pr[Mac\text{-}forge_{\mathcal{A},\Pi}(n) = 1] \leq 2^{-n} + \text{negl}(n). \quad (3)$$

□

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The domain extension problem

- Message length needs to be equal to the underlying PRF's input length in Construction 4.5.
- Existing practical PRFs (i.e. block ciphers) take short, fixed-length inputs. (e.g. AES takes 128-bit input only.)

Q: Given a fixed-length MAC_k , how to extend it to handle longer messages?

Trial 1: authenticating separately

Given a MAC_k of a fixed-length n ,

- Break the long message M into multiple short blocks m_1, \dots, m_d of fixed length n .
- **Authenticate each block separately**, i.e. compute $t_i = MAC_k(m_i)$ for all i , and output $\langle t_1, \dots, t_d \rangle$ as the tag.

Q: Is this secure? Why?

Trial 1 is NOT secure

Given a MAC_k of a fixed-length n ,

- Break the long message M into multiple short blocks m_1, \dots, m_d of fixed length n .
- **Authenticate each block separately**, i.e. compute $t_i = MAC_k(m_i)$ for all i , and output $\langle t_1, \dots, t_d \rangle$ as the tag.

Q: Is this secure? Why?

A: No, an attacker can launch a “**block reordering attack**” e.g. generate a new message-tag pair $\langle m_2 || m_1, t_2 || t_1 \rangle$ after seeing a correct pair $\langle m_1 || m_2, t_1 || t_2 \rangle$.

Trial 2: adding index

Given a MAC_k of a fixed-length n ,

- Break the long message M into multiple short blocks m_1, \dots, m_d of fixed length.
- **Authenticate each block along with its index separately**, i.e. compute $t_i = MAC_k(i || m_i)$ for all i , and output $\langle t_1, \dots, t_d \rangle$ as the tag.

Q: Is this secure? Why?

Trial 2 is NOT secure

Given a MAC_k of a fixed-length n ,

- Break the long message M into multiple short blocks m_1, \dots, m_d of fixed length.
- **Authenticate each block along with its index separately**, i.e. compute $t_i = MAC_k(i || m_i)$ for all i , and output $\langle t_1, \dots, t_d \rangle$ as the tag.

Q: Is this secure? Why?

A: No, an attacker can launch a “**truncation attack**”, e.g. generate a new message-tag pair $\langle m_1, t_1 \rangle$ after seeing a correct pair $\langle m_1 || m_2, t_1 || t_2 \rangle$.

Trial 3: Adding message length

Given a MAC_k of a fixed-length n ,

- Break the long message M into multiple short blocks m_1, \dots, m_d of fixed length.
- **Authenticate each block along with its index and the message length separately**, i.e. compute $t_i = MAC_k(d||i||m_i)$ for all i , and output $\langle t_1, \dots, t_d \rangle$ as the tag.

Q: Is this secure? Why?

Trial 3: Adding message length

Given a MAC_k of a fixed-length n ,

- Break the long message M into multiple short blocks m_1, \dots, m_d of fixed length n .
- **Authenticate each block along with its index and the message length separately**, i.e. compute $t_i = MAC_k(d||i||m_i)$ for all i , and output $\langle t_1, \dots, t_d \rangle$ as the tag.

Q: Is this secure? Why?

A: No, an attacker can launch a “**mix-and-match attack**”, e.g. generate a new message-tag pair $\langle m_1||m'_2, t_1||t'_2 \rangle$ after seeing two correct pairs $\langle m_1||m_2, t_1||t_2 \rangle$ and $\langle m'_1||m'_2, t'_1||t'_2 \rangle$.

CBC-MAC for domain extension

- Trial 3 can be fixed by further including a unique “message identifier”, however, it still has a big drawback of “long tag”, i.e. the tag is as long as the message.
- In practice, a standardized MAC that is used widely is **CBC-MAC**.

The basic CBC-MAC

When authenticating messages of any **fixed** length, one can use:

Construction 4.11: Basic CBC-MAC for fixed-length messages

Let F be a pseudorandom function, and fix a length function $l > 0$:

- *Mac*: on input a key $k \in \{0, 1\}^n$ and a message of length $l(n) \cdot n$,
 - 1 Parse $m = m_1, \dots, m_l$ where each m_i is of length n .
 - 2 Set $t_0 := 0^n$. Then, for $i = 1$ to l :
Set $t_i := F_k(t_{i-1} \oplus m_i)$.

Output t_l as the tag.

- *Vrfy*: on input a key $k \in \{0, 1\}^n$, a message m , and a tag t , do: If m is not of length $l(n) \cdot n$ then output 0. Otherwise, output 1 if $t = \text{Mac}_k(m)$.

The security of basic CBC-MAC

Regarding the security, we have

THEOREM 4.12

Let l be a polynomial. If F is a pseudorandom function, then Construction 4.11 is a secure MAC for messages of length $l(n) \cdot n$.

- We caution that the basic CBC-MAC is **NOT secure** in the general case when messages of different lengths may be authenticated. In such case, a variant of CBC-MAC can be used.
- Read the proof and also the variant in textbook if you are interested.

CBC-MAC v.s. CBC-mode encryption

Despite the similarities, they have important differences:

- CBC-mode encryption uses a **random IV (crucial for security)**;
CBC-MAC uses **NO IV** or a **fixed zero-IV** (also **crucial for security**).
- CBC-mode encryption output all blocks; CBC-MAC only output **the final block (crucial for security)**

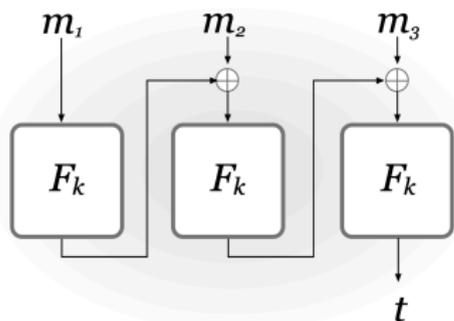


图 6: The basic CBC-MAC

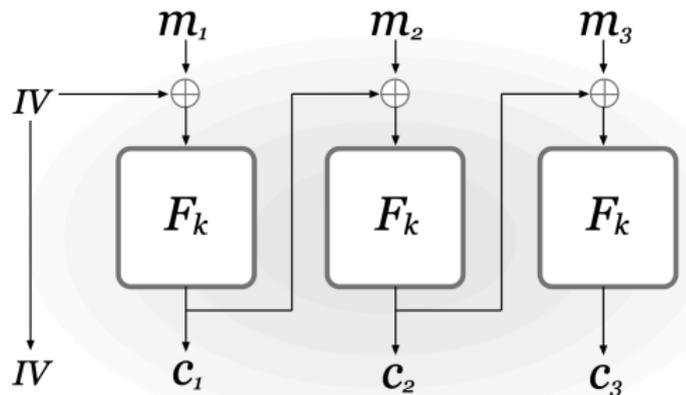


图 7: CBC mode of operation

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- **Definition of AE**
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Achieving secrecy and integrity simultaneously

- We have shown how to obtain **secrecy** in private-key setting using **encryption**.
- We have just shown how to obtain **integrity** using **MAC**.

Q: How can we achieve both goals **simultaneously**?

A: We resort to **Authenticated Encryption** (AE).

Definition of AE

To achieve an “ideally secure” communication, we require AE can simultaneously protect:

- data secrecy: Specifically, we require AE to be **CCA-secure**.
- data integrity: Specifically, we require AE to be **unforgeable**.

DEFINITION 4.17

A private-key encryption is an **authenticated encryption** scheme if it is **CCA-secure** and **unforgeable**.

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The CCA indistinguishability experiment

To formalize our secrecy goal, we first define the following experiment:

The CCA indistinguishability experiment $\text{PrivK}_{\mathcal{A}, \Pi}^{\text{cca}}(n)$:

- 1 A key k is generated by running $\text{Gen}(1^n)$.
- 2 Adversary \mathcal{A} is given input 1^n and oracle access to $\text{Enc}_k(\cdot)$ and $\text{Dec}_k(\cdot)$. It outputs a pair of messages m_0, m_1 of the same length.
- 3 A uniform bit $b \in \{0, 1\}$ is chosen, and then a ciphertext $c \leftarrow \text{Enc}_k(m_b)$ is computed and given to \mathcal{A} . We call c the challenge ciphertext.
- 4 The adversary \mathcal{A} continues to have oracle access to $\text{Enc}_k(\cdot)$ and $\text{Dec}_k(\cdot)$, but is **not allowed to query the latter on the challenge ciphertext** itself. Eventually, \mathcal{A} outputs a bit b' .
- 5 The output of the experiment is defined to 1 if $b' = b$, and 0 otherwise. If the output of the experiment is 1, we say that \mathcal{A} **succeeds**.

DEFINITION 3.33

A private-key encryption scheme Π has **indistinguishable encryption under a chosen-ciphertext attack**, or is **CCA-secure**, if for all PPT adversaries \mathcal{A} there is a negligible function $negl$ such that:

$$Pr[PrivK_{\mathcal{A}, \Pi}^{cca}(n) = 1] \leq \frac{1}{2} + negl(n), \quad (4)$$

where the probability is taken over all randomness used in the experiment.

An example of non-CCA-secure encryption

- Is the following construction CCA-secure? No!

Construction 3.30: A CPA-secure scheme from any pseudo-random function

Let F be a pseudorandom function. Define a private-key encryption scheme for messages of length n as follows:

- *Gen*: on input 1^n , choose uniform $k \in \{0, 1\}^n$ and output it.
- *Enc*: on input a key $k \in \{0, 1\}^n$ and a message $m \in \{0, 1\}^n$, choose uniform $r \in \{0, 1\}^n$ and outputs the ciphertext

$$c := \langle r, F_k(r) \oplus m \rangle .$$

- *Dec*: on input a key $k \in \{0, 1\}^n$ and a ciphertext $c = \langle r, s \rangle$, output the plaintext message

$$m := F_k(r) \oplus s$$

CCA-secureness implies “non-malleability”

- An encryption algorithm is **malleable** means one can generate a new ciphertext based on a ciphertext of m **without knowing m** , and the new ciphertext' corresponding plaintext is $f(m)$ for a known function f .
- Example: Given $c = \langle c_1 = r, c_2 = F_k(r) \oplus m \rangle$, adversary can construct

$$c' = \langle c_1, c_2 \oplus a \rangle$$

which decrypts to $m \oplus a$.

- A CCA-adversary can query c' 's decryption, gets $m \oplus a$ and m .
- **CCA-secureness implies “non-malleability” (“不可延展性” 或 “不可锻造性”)**.

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The unforgeable encryption experiment

To formalize our integrity goal, we define the following experiment:

The unforgeable encryption experiment $Enc\text{-}Forge_{\mathcal{A},\Pi}(n)$:

- 1 Run $Gen(1^n)$ to obtain a key k .
- 2 The adversary \mathcal{A} is given input 1^n and access to an encryption oracle $Enc_k(\cdot)$. The adversary outputs a ciphertext c .
- 3 Let $m := Dec_k(c)$, and let \mathcal{Q} denote the set of all queries that \mathcal{A} asked its encryption oracle. The output of the experiment is 1 iff (1) $m \neq \perp$ (i.e. decryption fails.) and (2) $m \notin \mathcal{Q}$ (i.e. m has not been queried.).

DEFINITION 4.16

A private-key encryption scheme Π is **unforgeable** if for all PPT adversaries \mathcal{A} , there is a negligible function $negl$ such that:

$$Pr[Enc-Forge_{\mathcal{A},\Pi}(n) = 1] \leq negl(n).$$

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Constructing AE via combining secure encryption scheme and AE

Our basic idea is to combine a CPA-secure encryption scheme and a MAC scheme to construct an AE. We have three different approaches to perform the combining:

- Encrypt-and-authenticate.
- Authenticate-then-encrypt
- Encrypt-then-authenticate

Encrypt and authenticate

Let $\Pi_E = (Enc, Dec)$ be an arbitrary CPA-secure encryption scheme and let $\Pi_M = (Mac, Vrfy)$ denote an arbitrary (strongly) secure MAC scheme, where key generation in both schemes simply involves choosing a uniform n -bit key.

Encrypt-and-authenticate:

- 1 The sender and the receiver agree on **independent** secret keys:

$$k_E \xleftarrow{\$} \{0, 1\}^n, k_M \xleftarrow{\$} \{0, 1\}^n.$$

- 2 For message m , sender computes

$$c \leftarrow Enc_{k_E}(m) \text{ and } t \leftarrow Mac_{k_M}(m),$$

and sends (c, t) to receiver.

- 3 Receiver decrypts c to recover m ; assuming no error occurred, it then verifies the tag t . If $Vrfy(m, t) = 1$, receiver outputs m ; otherwise, it outputs an error.

Possible weakness of Encrypt-and-authenticate

Weakness of AEs constructed using this approach?

- Message secrecy is NOT necessarily protected (as a secure MAC does NOT guarantee any secrecy.).
- Specifically, the encrypt-and-authenticate scheme is likely to be insecure against chosen-plaintext attack (since most MAC used in practice are deterministic.).

Note: the above analysis assumes a very general setting (where an arbitrary CPA-secure encryption and an arbitrary secure MAC are adopted). It does not mean the encrypt-and-authenticate cannot protect message secrecy under all circumstances.

Authenticate then encrypt

Let $\Pi_E = (Enc, Dec)$ be an arbitrary CPA-secure encryption scheme and let $\Pi_M = (Mac, Vrfy)$ denote an arbitrary (strongly) secure MAC scheme, where key generation in both schemes simply involves choosing a uniform n -bit key.

Authenticate-then-encrypt:

- 1 The sender and the receiver agree on **independent** secret keys:

$$k_E \xleftarrow{\$} \{0, 1\}^n, k_M \xleftarrow{\$} \{0, 1\}^n.$$

- 2 For message m , sender computes

$$t \leftarrow Mac_{k_M}(m) \text{ and } c \leftarrow Enc_{k_E}(m||t),$$

and sends c to receiver.

- 3 Receiver decrypts c to recover $m||t$; assuming no error occurred, it then verifies the tag t . If $Vrfy(m, t) = 1$, receiver outputs m ; otherwise, it outputs an error \perp .

Possible weakness of Authenticate-then-encrypt

- Ciphertext integrity is NOT protected.
- Thus, the adversary may be able to manipulate the ciphertext. In addition, the receiver has to first decrypt and then know whether the message is authentic or not.
- The above facts have be utilized to launch attacks, e.g. Padding oracle attacks, POODLE attacks and Lucky 13 for historical SSL and TLS protocol.
- **Authenticate-then-encrypt does not provide AE in general, and should NOT be used.**

Encrypt then authenticate

Let $\Pi_E = (Enc, Dec)$ be an arbitrary CPA-secure encryption scheme and let $\Pi_M = (Mac, Vrfy)$ denote an arbitrary (strongly) secure MAC scheme. Define a private-key encryption scheme (Gen', Enc', Dec') as follows.

CONSTRUCTION 4.18 (Encrypt-then-authenticate):

- 1 Gen' : on input 1^n , $k_E \xleftarrow{\$} \{0, 1\}^n$, $k_M \xleftarrow{\$} \{0, 1\}^n$.
- 2 Enc' : on input a key (k_E, k_M) and plaintext m , computes

$$c \leftarrow Enc_{k_E}(m) \text{ and } t \leftarrow Mac_{k_M}(c).$$

Output the ciphertext $\langle c, t \rangle$.

- 3 Dec' : on input a key (k_E, k_M) and ciphertext $\langle c, t \rangle$, outputs \perp if $Vrfy(c, t) \neq 1$, and otherwise, outputs $Dec_{k_E}(c)$.

THEOREM 4.19

Let Π_E be a CPA-secure encryption scheme and let Π_M be a strongly secure MAC scheme. Then Construction 4.18 is an authenticated encryption scheme.

Why is it true?

- Strong security of Π_M directly implies Construction 4.18 is unforgeable.
- CCA-security of Construction 4.18 reduces to the CPA-security of Π_E .

“Among the three, Encrypt-then-Authenticate is the most ideal approach to construct an AE.”



Katz, J. and Lindell, Y..

Chapter 4 of “Introduction to modern cryptography” (2nd ed).

Chapman & Hall/CRC, 2014